

# Strong forward security in signcryption schemes

Madeline González Muñiz



# What is Signcryption?

- ✿ Sign-then-Encrypt for authenticity and confidentiality
- ✿ Combine both and achieve efficiency with signcryption primitive
- ✿ Goal: Achieve confidentiality, unforgeability, and non-repudiation
- ✿ Setup has sender and receiver
  - ✿ Let Alice be the sender
  - ✿ Let Bob be the receiver
  - ✿ Let Eve be an adversary

# Scheme Setup

- ✿ Signcryption scheme  $\mathbf{SC}=\{K, SE, VD\}$ ,  $\mathbf{U}=\{SK_U, PK_U\}$
- ✿ Correctness  $VD_B(c)=m$  for  $c=SE_A(m)$ 
  - ✿ Alice computes  $SE_A(m)$  using  $SK_A, PK_B$
  - ✿ Bob computes  $VD_B(c)$  using  $SK_B, PK_A$

# Outsider Security

- ☼ Eve has access to the public keys of Alice and Bob

- ☼ EUF-CMA

- ☼ Eve has to come up with a valid signcryption of new message  $m$  that Bob designcrypts successfully

- ☼ IND-CCA

- ☼ Eve chooses two messages, one of which is signcrypted and Eve must guess which one

# Insider Security

- ☀ Induced signature scheme from **SC**

- ☀ Signing key is  $SK_A, PK_B$

- ☀ Verification key is  $SK_B, PK_A$

- ☀ Make  $SK_B$  public

- ☀ Induced encryption scheme from **SC**

- ☀ Encryption Key is  $SK_A, PK_B$

- ☀ Make  $SK_A$  public

- ☀ Decryption Key is  $SK_B, PK_A$

- ☀ Apply EUF-CMA, IND-CCA security definitions to induced schemes

# Bilinear Map

✿ Let  $G_1$  (additive) and  $G_2$  (multiplicative) be two groups of prime order  $q$  and  $e: G_1 \times G_1 \rightarrow G_2$  a bilinear map:

1. Bilinear: for all  $P, Q$  in  $G_1$ , for all  $a, b$  in  $\mathbb{Z}_q^*$ ,  
 $e(aP, bQ) = e(P, Q)^{ab}$
2. Non-degenerate: for any  $P$  in  $G_1$ ,  $e(P, Q) = 1$  for all  $Q$  in  $G_1$  iff  $P = 0$
3. Computable: there exists an efficient algorithm to compute  $e(P, Q)$  for all  $P, Q$  in  $G_1$

# Bilinear Diffie-Hellman Problem

- ✿ For  $G_1$ ,  $G_2$ ,  $q$ , and  $e$  as described in the previous slide, and a generator  $P$  of  $G_1$ , the BDHP is to compute  $e(P, P)^{abc}$  given  $(P, aP, bP, cP)$ .
- ✿ The decisional bilinear Diffie-Hellman Problem is to decide whether  $h = e(P, P)^{abc}$  for given  $(P, aP, bP, cP)$  and  $h$  in  $G_2$ .

# Identity-Based Cryptography

- ✿ User identifier information serves as a public key (such as email address)
- ✿ Trusted third party is the Private Key Generator
- ✿ Using the public key of the PKG and Bob's identity, Alice can encrypt to Bob
- ✿ Using the public key of the PKG and Alice's identity, Bob can verify signatures from Alice



# Example: Signcryption Scheme

Let  $H_1: \{0, 1\}^* \rightarrow G_1$ ,  $H_2: G_2 \rightarrow \{0, 1\}^n$ ,  $H_3: \{0, 1\}^* \times G_2 \rightarrow Z_q$

$$P_{pub} = sP, Q_{ID} = H_1(ID), d_{ID} = sQ_{ID}$$

<b>Signcrypt</b> : to send a message $m$ to Bob, Alice follows the steps below	<b>Unsigncrypt</b> : when receiving $\sigma = (c, r, S)$ , Bob performs the following tasks
<ol style="list-style-type: none"> <li>1. Compute <math>Q_{ID_B} = H_1(ID_B) \in G_1</math>.</li> <li>2. Choose <math>x \leftarrow_R \mathbb{F}_q^*</math>, and compute <math>k_1 = \hat{e}(P, P_{pub})^x</math> and <math>k_2 = H_2(\hat{e}(P_{pub}, Q_{ID_B})^x)</math>.</li> <li>3. Compute <math>c = E_{k_2}(m)</math>, <math>r = H_3(c, k_1)</math> and <math>S = xP_{pub} - rd_{ID_A} \in G_1</math>.</li> </ol>	<ol style="list-style-type: none"> <li>1. Compute <math>Q_{ID_A} = H_1(ID_A) \in G_1</math></li> <li>2. Compute <math>k_1 = \hat{e}(P, S)\hat{e}(P_{pub}, Q_{ID_A})^r</math></li> <li>3. Compute <math>\tau = \hat{e}(S, Q_{ID_B})\hat{e}(Q_{ID_A}, d_{ID_B})^r</math> and <math>k_2 = H_2(\tau)</math>.</li> <li>4. Recover <math>m = D_{k_2}(c)</math> and accept <math>\sigma</math> if and only if <math>r = H_3(c, k_1)</math>.</li> </ol>
<p>The ciphertext is <math>\sigma = (c, r, S)</math>.</p>	

# Public Ciphertext Verifiability

- ✿ Why not public message verifiability?
- ✿ In the IND-CCA game, Eve selects messages  $m_1$  and  $m_2$ .
- ✿ Eve gets a signcryption of  $m_1$  or  $m_2$
- ✿ With public message verifiability, Eve can check whether  $m_1$  or  $m_2$  was signcrypted, thus distinguishing
- ✿ For non-repudiation of message  $m$ , use zero-knowledge proof

# Forward Security

- ✿ Forward security in encryption schemes
  - ✿ Compromise of the current secret key does not allow an adversary to decrypt in the past
- ✿ Forward security in signature schemes
  - ✿ Compromise of the current secret key does not allow an adversary to forge in the past
- ✿ Strong forward security in signcryption achieves both

# Example: Signcryption Scheme with Encryption Forward Security

- ☀ Note that only Bob can recover  $e(R, d_B)$  since Alice cannot recover  $r$  from  $R$ .

**Authenticrypt :** to send a message  $m$  to Bob, Alice follows the steps below

1. Compute  $Q_{ID_B} = H_1(ID_B) \in \mathbb{G}_1$ .
2. Choose  $x \leftarrow_R \mathbb{F}_q^*$ , and compute  $(k_1, k_2) = H_2(\hat{e}(P_{pub}, Q_{ID_B})^x)$ .
3. Compute  $c = E_{k_2}(m)$ ,  $r = H_3(c, k_1)$ ,  
 $S = xP_{pub} - rd_{ID_A} \in \mathbb{G}_1$   
and  $R = rQ_{ID_A}$ .

The ciphertext is  $\sigma = (c, R, S)$ .

**Authentidecrypt :** when receiving  $\sigma = (c, R, S)$ , Bob performs these tasks

1. Compute  $Q_{ID_A} = H_1(ID_A) \in \mathbb{G}_1$ .
2. Compute  $\tau = \hat{e}(S, Q_{ID_B})\hat{e}(R, d_{ID_B})$   
and  $(k_1, k_2) = H_2(\tau)$ .
3. Recover  $m = D_{k_2}(c)$ .
4. Compute  $r = H_3(c, k_1)$  and  $rQ_{ID_A}$ .
5. Accept  $\sigma$  if and only if  $R = rQ_{ID_A}$ .

# Non-Interactive Key Exchange

- ✿ Using pairings Alice and Bob can non-interactively compute a secret key in the identity-based setting:
  - ✿ Alice computes  $e(d_A, Q_B)$
  - ✿ Bob computes  $e(Q_A, d_B)$
  - ✿  $e(d_A, Q_B) = e(sQ_A, Q_B) = e(Q_A, Q_B)^s = e(Q_A, sQ_B) = e(Q_A, d_B)$
- ✿ If the state of either Alice or Bob is compromised, the shared secret key is also compromised

# Partial Forward Secret Key Exchange

- ✿ Alice does the following:
  - ✿ Computes  $Q_B$
  - ✿ Randomly selects  $x$  in  $\mathbb{Z}_q^*$
  - ✿  $k_t = H_2(e(P_{pub}, Q_B)^x)$
  - ✿ Sets  $r = H_2(t, k_t)$ ,  $R = rQ_A$ , and  $S = xP_{pub} - rd_A$
  - ✿ Sends Bob  $(t, R, S)$
- ✿ If the sender's state becomes compromised, still secure because Alice cannot recover  $r$  given  $R$



# Partial Forward Secret Key Exchange

- ✿ Bob can do the same for randomly selected  $x'$  in  $Z_q^*$  and  $(t, R', S')$  where  $R' = r' Q_B$
- ✿ Then the agreed key becomes  $k_t = e(rd_A, R') = e(R, r' d_B)$
- ✿ If either the sender or receiver's state becomes compromised, still secure because Alice cannot recover  $r$  given  $R$  and Bob cannot recover  $r'$  given  $R'$
- ✿ What if both states are compromised?

# Partial Forward Secret Key Exchange

- ✿ What if both states are compromised?
- ✿ Alice needs to encrypt to Bob in a way that he cannot decrypt past messages, and vice versa
- ✿ We need forward-secure encryption



# Forward-Secure Encryption

- ✿ Recall that compromise of the current secret key does not allow an adversary to decrypt in the past
- ✿ Decryption keys are generated via one-way functions in such a way that even the rightful user cannot decrypt in the past
- ✿ Seed used to generate the decryption keys may be stored in a separate/secure device to recover decryption keys from past periods
- ✿ Canetti et al. make use of binary trees to create a forward-secure encryption scheme

# Strong Forward-Secure Signcryption

- ✿ Use the concept of a binary tree so that each user updates their secret key
- ✿ Alice and Bob can signcrypt messages to each other in such a way that an adversary cannot decrypt nor forge in the past

# Küsimused?